

Exploring Complexity Reduction in Deep Learning

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Key contributions

Pre-defined Sparsity

- Reduce complexity of NNs
- Guidelines for designing sparse NNs
- Hardware architecture for on-device training and inference

Automated Machine Learning: Deep-n-Cheap

- Target performance and training complexity
- Benchmark and custom datasets, CNNs and MLPs
- Insights into search process

Dataset Engineering

- Family of synthetic datasets
- Dataset difficulty metrics

Outline



Introduction and Background

Deep Learning

Machine Learning Neural Networks

Smart Systems





Artificial

Intelligence









A Quick Primer on Neural Networks (NN101) Feedforward 3 `ى: 48 365 -5 -4 7 0.5 **ERROR** `O_{.S} 2 6.4 0.3 Dog TRAINING

Learn network parameters — weights



Learn network parameters — weights



Learn network parameters — weights

NNs can be used for classification



TESTING / INFERENCE

Use learned network parameters

Measure accuracy performance — % of correctly classified test samples

Types of NNs – Multilayer Perceptron (MLP)



Fully connected (FC) – every node connects to every adjacent node

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Types of NNs – Convolutional Neural Network (CNN)



Convolution

technically it's correlation... but since when do engineers bother about math? Pooling Batch (Downsampling) Normalization

Dropout

The Complexity Conundrum...

Modern neural networks suffer from parameter explosion



He 2016

Training can take weeks on CPU

Cloud GPU resources are expensive



Google Cloud Platform



... and the Design Conundrum

- Deep neural networks have a lot of hyperparameters
 - How many layers? Architecture
 How many neurons? Hyperparameters
 Learning rate Training
 Batch size Hyperparameters
 and more...



• Our understanding of NNs is at best vague, at worst, zero!

The big question my research aims to answer

Can we reduce the storage and computational (which translate to temporal, financial and environmental) burden of deploying NNs, particularly the training phase, while minimizing performance degradation?



MIT Technology Review

Strubell 2019

Artificial intelligence / Machine learning

Training a single Al model can emit as much carbon as five cars in their lifetimes

Deep learning has a terrible carbon footprint.

Pre-Defined Sparsity

https://github.com/souryadey/predefinedsparse-nnets

Motivation behind pre-defined sparsity



In a FC MLP network, most weights are small in magnitude after training

Pre-defined Sparsity

Pre-define a sparse connection pattern **prior to training**

Use this sparse network for both training and inference

Reduced training and inference complexity



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Pre-defined sparsity performance on MLPs



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Designing pre-defined sparse networks

A pre-defined sparse connection pattern is a **hyperparameter** to be set prior to training

Find trends and guidelines to optimize pre-defined sparse patterns



1. Individual junction densities



Latter junctions (closer to the output) learn higher-order, more complicated representations => They need to be denser

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Results

Each curve keeps $\rho_{\rm 2}$ fixed and varies $\rho_{\rm net}$ by varying $\rho_{\rm 1}$

For the same ρ_{net} , $\rho_2 > \rho_1$ improves performance

Mostly similar trends observed for deeper networks



40

ρ₂ (%)

100 20

50

2. Dataset redundancy





Results

Reducing redundancy leads to increased performance degradation on sparsification

Pre-defined sparse design is problem-dependent



3. 'Large sparse' vs 'small dense' networks

A sparser network with more hidden nodes will outperform a denser network with less hidden nodes, when both have same number of weights



Results

Networks with same number of parameters go from bad to good as #nodes in hidden layers is increased





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4. Regularization – Why does pre-defined sparsity work?

$$C(\boldsymbol{w}) = C_0(\boldsymbol{w}) + \lambda \|\boldsymbol{w}\|_2^2$$

egularized cost
Original unregularized
cost (like cross-entropy)
Regularization term

Pre-defined sparse networks need smaller λ (as determined by validation)

| Overall Density | λ |
|------------------------|------------------------|
| 100 % | 1.1 x 10-4 |
| 40 % | 5.5 x 10 ⁻⁵ |
| 11 % | 0 |

Example for MNIST 2-junction networks

Pre-defined sparsity reduces the overfitting problem stemming from over-parametrization in big networks

R

Degree of parallelism (z) = Number of weights processed in parallel in a junction



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Operational parallelization and junction pipelining



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Prototype implemented on FPGA



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Operational parallelization and junction pipelining

Prototype implemented on FPGA

Transferred to and currently being developed by team SAPIENT, in collaboration with DTRA and USC ISI.



Automated Machine Learning : Deep-n-Cheap

https://github.com/souryadey/deep-n-cheap
AutoML (Automated Machine Learning)

- Software frameworks that make design decisions
- Given a problem, **search** for NN models



Jin 2019 – Auto-Keras





Mendoza 2018 – Auto-PyTorch

Our Work

Deep-n-Cheap

Low Complexity AutoML framework

Reduce training complexity

Target custom datasets and user requirements

Supports CNNs and MLPs

| Framowork | Architactura soarch space | Training | Adjust model | |
|--------------|---------------------------------|------------|-----------------------------|---|
| FIAMEWORK | Architecture search space | hyp search | $\operatorname{complexity}$ | |
| Auto-Keras | Only pre-existing architectures | No | No | |
| AutoGluon | Only pre-existing architectures | Yes | No | |
| Auto-PyTorch | Customizable by user | Yes | No | t _{tr} = Training time / epoch |
| Deep-n-Cheap | Customizable by user | Yes | Penalize $t_{\rm tr}, N_p$ | N _p = # Trainable parameters |

Search Objective

Optimize performance and complexity

Modified loss function: $f(NN Config \mathbf{x}) = \log(f_p + w_c^* f_c)$

Example config **x**: [#layers, #channels] = [3, (29,40,77)]

$$\begin{split} f_{\rho} &= 1 - (\text{Best Validation Accuracy}) \\ f_{c} &= \text{Normalized } t_{tr} \text{ or } \text{N}_{\rho} \\ &= \text{t}_{\text{tr}}(\text{config}) \ / \ \text{t}_{\text{tr}}(\text{baseline}) \end{split}$$











Α

Examples of Stage 2



Full shortcuts (left) Half shortcuts (right)



Bayesian Optimization Workflow Model function f

- Sample some initial data $X_{1:n1}$ and find $f(X_{1:n1})$
- Form prior to approximate f. This is a *Gaussian process* with μ_{n1x1} , Σ_{n1xn1}
- Repeat for n2 steps:
 - Sample new points X'_{1:n3}
 - Find *expected improvement* EI(**x**') for each new point and choose **x**_{n1+1} = argmax EI(**x**')
 - Form *posterior* to approximate f :
 - Augment $\mathbf{X}_{1:n1}$ to $\mathbf{X}_{1:n1+1}$
 - Find f(**x**_{n+1})
 - Augment $\boldsymbol{\mu}_{n1x1}$ to $\boldsymbol{\mu}_{(n1+1)x1}$, $\boldsymbol{\Sigma}_{n1xn1 \text{ to}} \boldsymbol{\Sigma}_{(n1+1)x(n1+1)}$
- Finally, return best f and corresponding best **x**

Total configs explored: n1 + n2*n3 Total configs trained: n1 + n2

Gaussian process (GP)

A collection of random variables such that any subset of them forms a multidimensional Gaussian random vector

$$f(\boldsymbol{X}_{1:n}) \sim \mathcal{N}\left(\boldsymbol{\mu}_{n \times 1}, \boldsymbol{\Sigma}_{n \times n}\right)$$

 $oldsymbol{\mu} = egin{bmatrix} \mu\left(oldsymbol{x}_1
ight) \ dots \ \mu\left(oldsymbol{x}_n
ight) \end{bmatrix}$

$$oldsymbol{\Sigma} = egin{bmatrix} \sigma\left(oldsymbol{x}_1,oldsymbol{x}_1
ight) & \cdots & \sigma\left(oldsymbol{x}_1,oldsymbol{x}_n
ight) \ dots & dots & dots & dots \ \sigma\left(oldsymbol{x}_n,oldsymbol{x}_1
ight) & \cdots & \sigma\left(oldsymbol{x}_n,oldsymbol{x}_n
ight) \end{bmatrix}$$

Covariance kernel – Similarity between NN configs

$$d(x_{ik}, x_{jk}) = \omega_k \left(\frac{|x_{ik} - x_{jk}|}{u_k - l_k}\right)^{r_k}$$



Individual

Distance

Covariance kernel – Similarity between NN configs

Individual Distance

$$d(x_{ik}, x_{jk}) = \omega_k \left(\frac{|x_{ik} - x_{jk}|}{u_k - l_k}\right)^{r_k}$$
$$\sigma(x_{ik}, x_{jk}) = \exp\left(-\frac{d^2(x_{ik}, x_{jk})}{2}\right)$$

Individual Kernel

Pre-decidedConfig
$$i$$
Config j ComputedImage: Second structureMin channels = 16
Max channels = 64
omega = 3, r = 150 channels36 channelsDistance = 0.875
Kernel = 0.682Image: Second structureMin channels = 16
Max channels = 128
omega = 3, r = 1/2S0 channels61 channelsDistance = 1.236
Kernel = 0.466Image: Second structureMin channels = 16
Max channels = 256
omega = 3, r = 1/3No 3rd layer107 channelsDistance = 3 (i.e. max)
Kernel = 0.01 (i.e. min)

2



Assuming all {s} are equal, final kernel value = 0.386

Expected Improvement (EI)

- Let f* be the minimum of all observed values so far
- How much can a new point **x** improve:
 - If $f(x) > f^*$, Imp(x) = 0
 - Else, Imp(x) = f*-f(x)
- EI(x) = Expectation [max(f*-f(x),0)]

$$EI(\boldsymbol{x}) = (f^* - \mu)P\left(\frac{f^* - \mu}{\sigma}\right) + \sigma p\left(\frac{f^* - \mu}{\sigma}\right)$$

Standard normal cdf = P, pdf = p

Don't need to evaluate f(x) to find El(x)

Data loader and augmentation considerations



npz is faster, data loaders are more versatile

CNN Results

Complexity Penalty = Training time / epoch

> AWS p3.2xlarge with 1 V100 GPU

We are not penalizing this, but it's correlated

Performancecomplexity tradeoff



CNN Results

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Softmax

CIFAR-10 w/ aug



| w _c | 0 | 0.01 | 0.1 | 1 | 10 |
|-------------------------|------------------------|------------------------|------------------------|-------|-------|
| Initial learning rate η | 0.001 | 0.001 | 0.001 | 0.003 | 0.001 |
| Weight decay λ | 3.3 x 10 ⁻⁵ | 8.3 x 10 ⁻⁵ | 1.2 x 10 ⁻⁵ | 0 | 0 |
| Batch size | 120 | 256 | 459 | 452 | 256 |

 λ strictly correlated with N_p

MLP Results

Pink dots: *Complexity Penalty =* Training time / epoch

Black crosses: *Complexity Penalty =* # Trainable Params

CPU = Macbook Pro with 8GB RAM, no CuDA GPU = (Same) AWS p3.2xlarge with V100





91

90

89

88

87

86

85

X

10k

5k

X

3

2

1

0

0

х

0.01

х

X

1

х

10

Х

×

х

0.1

 W_c

10

1

Reuters RCV1 on GPU

× 😞



S

10k

5k

Search cost (CPU/GPU hrs) 1 ⁷ ⁵ ⁵ ⁵

0

0

х

0.01 0.1

х

 W_c



х





91.4 🗙

91.2

91.0

90.8

90.6

90.4





MLP Results

Pink dots: *Complexity Penalty =* Training time / epoch

Black crosses: *Complexity Penalty =* # Trainable Params

CPU = Macbook Pro with 8GB RAM, no CuDA GPU = (Same) AWS p3.2xlarge with V100



500k 😾

100k

50k

10k

5k

Search cost (CPU/GPU hrs) 1 ⁷ ⁵ ⁵ ⁵

0

0

S

MNIST on CPU



Fashion MNIST on CPU

Reuters RCV1 on GPU

-×

×

× 😞

91.4 🗙

91.2

91.0

90.8

Running Deep-n-Cheap

How to run?

- Install Python 3
- Install Pytorch
- \$ pip install sobol_seq tqdm
- \$ git clone https://github.com/souryadey/deep-n-cheap.git
- \$ cd deep-n-cheap
- \$ python main.py

For help:

\$ python main.py -h

Datasets (including custom)

Set dataset to either:

 --dataset=torchvision.datasets.<dataset> . Currently supported values of <dataset> = MNIST, FashionMNIST, CIFAR10, CIFAR100

DnC

- --dataset='<dataset>.npz', where <dataset> is a .npz file with 4 keys:
 - xtr : numpy array of shape (num_train_samples, num_features...), example (50000,3,32,32) or (60000,784). Image data should be in *channels_first* format.
 - ytr : numpy array of shape (num_train_samples,)
 - xte : numpy array of shape (num_test_samples, num_features...)
 - yte : numpy array of shape (num_test_samples,)
- Some datasets can be downloaded from the links in dataset_links.txt. Alternatively, define your own custom datasets.

Comparison (CNNs on CIFAR-10)

| Framowork | Additional | Search cost | Best model found from search | | | |
|---------------|--------------|-------------|------------------------------|----------------------|------------|---------------------|
| | settings | (GPU hrs) | Architecture | $t_{ m tr}~(m sec)$ | Batch size | Best val acc $(\%)$ |
| Proxyless NAS | Proxyless-G | 96 | 537 conv layers | 429 | 64 | 93.22 |
| Auto-Keras | Default run | 14.33 | Resnet-20 v2 | 33 | 32 | 74.89 |
| AutoCluon | Default run | 3 | Resnet-20 v1 | 37 | 64 | 88.6 |
| AutoGluon | Extended run | 101 | Resnet-56 v1 | 46 | 64 | 91.22 |
| Auto-Pytorch | 'tiny cs' | 6.17 | 30 conv layers | 39 | 64 | 87.81 |
| Auto-1 ytoren | 'full cs' | 6.13 | 41 conv layers | 31 | 106 | 86.37 |
| | $w_c = 0$ | 29.17 | 14 conv layers | 10 | 120 | 93.74 |
| Deep-n-Cheap | $w_c = 0.1$ | 19.23 | 8 conv layers | 4 | 459 | 91.89 |
| | $w_c = 10$ | 16.23 | 4 conv layers | 3 | 256 | 83.82 |

Penalizes inference complexity, <u>not</u> training

Auto Keras and Gluon don't support getting final model out, so we compared on best val accfound during search instead of final test acc

Comparison (MLPs)

| Framework Additional Search cost Best model found from search | | | | arch | | | |
|---|-------------|-----------|------------|--------------|----------------------|------------|---------------------|
| Flamework | settings | (GPU hrs) | MLP layers | N_p | $t_{ m tr}~(m sec)$ | Batch size | Best val acc $(\%)$ |
| | | | Fashion MN | IST | | | |
| | 'tiny cs' | 6.76 | 50 | 27.8M | 19.2 | 125 | 91 |
| Auto-Pytorch | 'medium cs' | 5.53 | 20 | 3.5M | 8.3 | 184 | 90.52 |
| | 'full cs' | 6.63 | 12 | 122k | 5.4 | 173 | 90.61 |
| Deep-n-Cheap | $w_c = 0$ | 0.52 | 3 | 263k | 0.4 | 272 | 90.24 |
| (penalize $t_{\rm tr}$) | $w_c = 10$ | 0.3 | 1 | 7.9 k | 0.1 | 511 | 84.39 |
| Deep-n-Cheap | $w_c = 0$ | 0.44 | 2 | 317k | 0.5 | 153 | 90.53 |
| (penalize N_p) | $w_c = 10$ | 0.4 | 1 | 7.9 k | 0.2 | 256 | 86.06 |
| Reuters RCV1 | | | | | | | |
| Auto-Pytorch | 'tiny cs' | 7.22 | 38 | 19.7M | 39.6 | 125 | 88.91 |
| Auto-1 ytoren | 'medium cs' | 6.47 | 11 | 11.2M | 22.3 | 337 | 90.77 |
| Deep-n-Cheap | $w_c = 0$ | 1.83 | 2 | 1.32M | 0.7 | 503 | 91.36 |
| (penalize $t_{\rm tr}$) | $w_c = 1$ | 1.25 | 1 | 100k | 0.4 | 512 | 90.34 |
| Deep-n-Cheap | $w_c = 0$ | 2.22 | 2 | 1.6M | 0.6 | 512 | 91.36 |
| (penalize N_p) | $w_c = 1$ | 1.85 | 1 | 100k | 5.54 | 33 | 90.4 |

Takeaway

We may not need very deep networks!

Also see Zagoruyko 2016 – WRN



Search transfer

Can a NN architecture found after stages 1 and 2 on dataset A be applied to dataset B after running Stage 3 training hyperparameter search?

How does it compare to native search on dataset B?

Can architectures generalize?



Search transfer results

Transferring from CIFAR outperforms native FMNIST (probably due to more params)

Training times mostly the same (a) CIFAR-10







Justifying our greed









Choosing initial points in Bayesian optimization



Random sampling



Sobol sampling Like grid search Better for more dimensions

BO vs random and grid search (30 points each)



Purely random search: 30 prior Purely grid search (Sobol): 30 prior

Balanced BO: 15 prior + 15 steps Extreme BO: 1 prior + 29 steps

Ensembling

Multiple models vote on final test samples



Slight increases in performance at the cost of large increases in complexity

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First release

souryadey released this 21 days ago · 7 commits to master since this release

Compare -

Version used for obtaining results for the paper -- S. Dey, S. C. Kanala, K. M. Chugg and P. A. Beerel, "Deepn-Cheap: An Automated Search Framework for Low Complexity Deep Learning", submitted to ECML-PKDD 2020.

| Assets 2 |
|----------------------|
| Source code (zip) |
| Source code (tar.gz) |

Extension to segmentation and RNNs coming soon

Edit

Dataset Engineering

https://github.com/souryadey/morse-dataset

Data, data, everywhere, Not quality enough to use

Real world data has challenges:

- ≻ Too few samples
- > Incorrect labeling
- \succ Missing entries





Synthetic data is generated using computer algorithms
➢ Very large quantities can be generated
➢ Mimic real-world data as desired
➢ Classification difficulty tweaking

Morse Code Datasets

| Step 1: | | | | | |
|-----------------------------------|--|--|--|--|--|
| Frame length: 64 | | | | | |
| Dot: 1-3 | | | | | |
| Dash: 4-9 | | | | | |
| Intermediate space: 1-3 | | | | | |
| Leading spaces: None | | | | | |
| Trailing spaces: Remaining at end | | | | | |



Codeword Length = 26. Remaining spaces = 38

Morse Code is a system of communication where letters, numbers and symbols are encoded using dots and dashes

Example:



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Morse Code Datasets

Morse Code is a system of communication where letters, numbers and symbols are encoded using dots and dashes

Example:





12,12,9,12,13,14,10

11,13,14,12,12
symbols are encoded

using dots and dashes

communication where

letters, numbers and

Morse Code

Datasets

Example:



Variations and Difficulty Scaling

- > More noise
- ➤ Leading and trailing spaces
- > Confusing dashes with dots and spaces
- > Dilating frame to size 256
- Increasing #samples in dataset \





Neural network performance (3-layer MLP)



Tunable dataset difficulty leads to a variety of benchmarks

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Metrics to characterize dataset difficulty



Goodness of the Metrics

| Metric | r | |
|------------------|-------|--|
| $V_{\rm lower}$ | -0.59 | |
| $V_{ m upper}$ | -0.64 | |
| $V_{\rm dist}$ | -0.63 | |
| $V_{\rm thresh}$ | -0.64 | |

Pearson's correlation coefficient between metric and test set classification accuracy of Morse code datasets of varying difficulty (negative because metrics indicate difficulty)

Metrics can be used to understand the inherent difficulty of the classification problem on a dataset before applying any learning algorithm

Publications

Sourya Dey

- S. Dey, S. C. Kanala, K. M. Chugg and P. A. Beerel, "Deep-n-Cheap: An Automated Search Framework for Low Complexity Deep Learning", submitted to *ECML-PKDD* 2020. Pre-print: <u>arXiv:2004.00974</u>.
- **S. Dey**, K. Huang, P. A. Beerel and K. M. Chugg, "Pre-Defined Sparse Neural Networks with Hardware Acceleration," in *IEEE JETCAS* 2019.
- S. Dey, K. M. Chugg and P. A. Beerel, "Morse Code Datasets for Machine Learning," in *ICCCNT* 2018. Won Best Paper Award.
- **S. Dey**, D. Chen, Z. Li, S. Kundu, K. Huang, K. M. Chugg and P. A. Beerel, "A Highly Parallel FPGA Implementation of Sparse Neural Network Training," in *ReConFig 2018*.
- **S. Dey**, K. Huang, P. A. Beerel and K. M. Chugg, "Characterizing sparse connectivity patterns in neural networks," in *ITA* 2018.
- S. Dey, P. A. Beerel and K. M. Chugg, "Interleaver design for deep neural networks," in ACSSC 2017.
- **S. Dey**, Y. Shao, K. M. Chugg and P. A. Beerel, "Accelerating training of deep neural networks via sparse edge processing," in *ICANN* 2017.

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Diandian Chen Former MS Student



Souvik Kundu PhD Student



Saikrishna C. Kanala

MS Student

... and many others!

Thank you!

https://souryadey.github.io/

